

AS3012:
Exoplanetary
Science

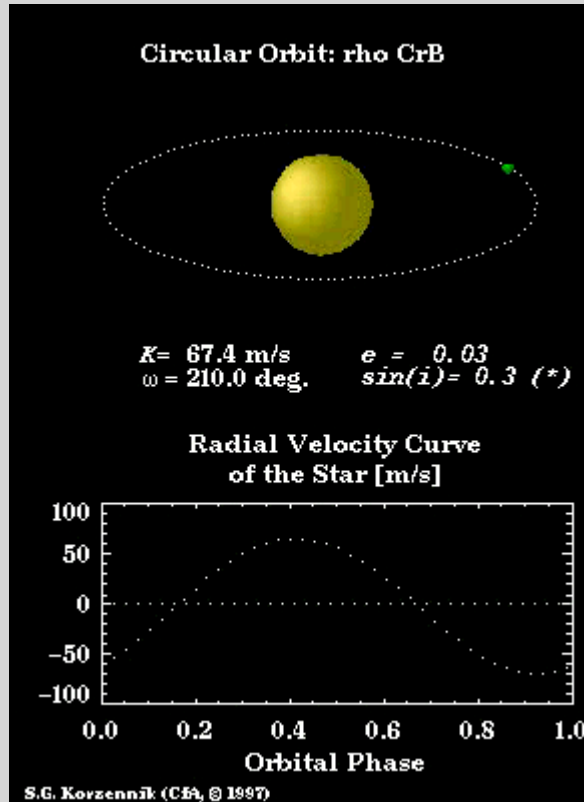


Stephen Kane

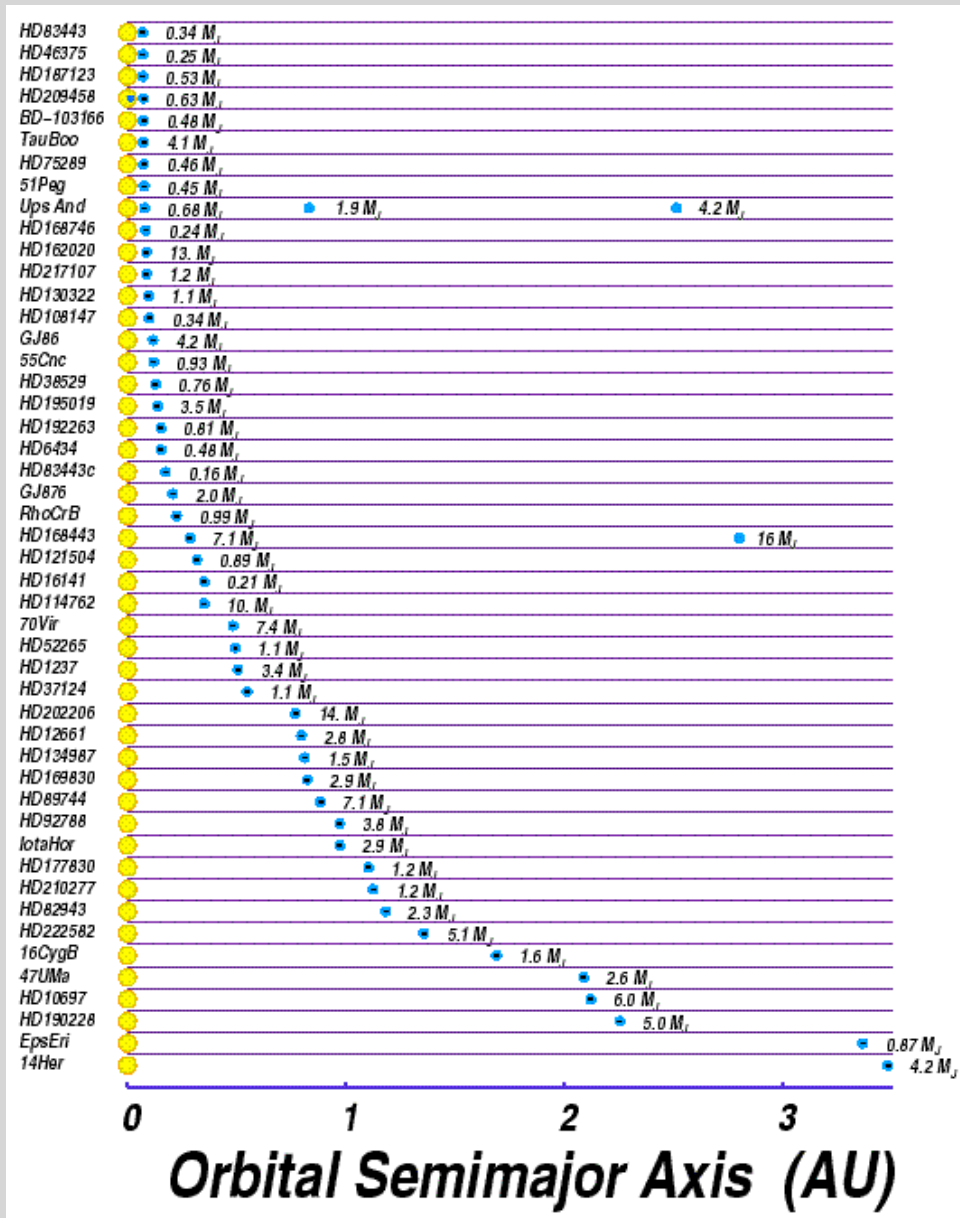
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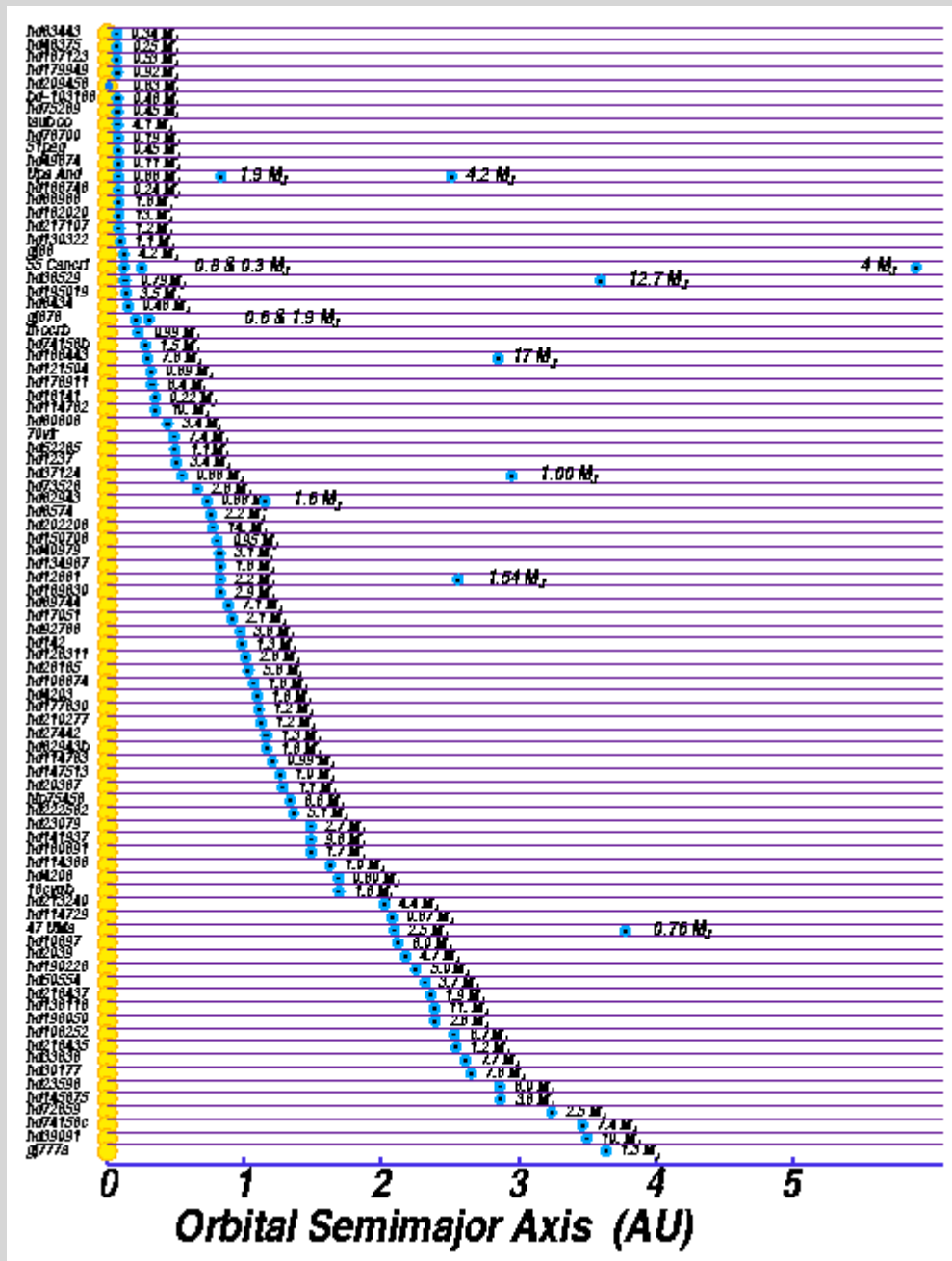
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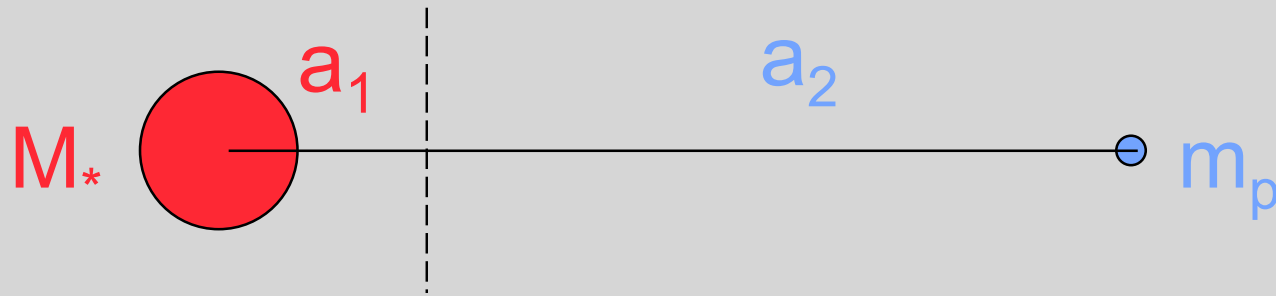
Radial velocities



- Currently the most successful method used to detect exoplanets
- Method relies on the Doppler shift of starlight resulting from the star orbiting a common center of mass with a companion planet







Centre of mass of
binary system

Planet in circular orbit around star with semi-major axis a

Star and planet both rotate around the centre of mass with
an angular velocity:

$$\Omega = \sqrt{\frac{G(M_* + m_p)}{a^3}}$$

Using $a_1 M_* = a_2 m_p$ and $a = a_1 + a_2$, stellar velocity in inertial frame is:

$$v_* \approx \left(\frac{m_p}{M_*} \right) \sqrt{\frac{GM_*}{a}}$$

(assuming $m_p \ll M_*$)

For a circular orbit, observe a sin-wave variation of the stellar radial velocity, with an amplitude that depends upon the inclination of the orbit to the line of sight:

$$v_{obs} = v_* \sin(i)$$

Hence, measurement of the radial velocity amplitude produces a constraint on:

$$m_p \sin(i)$$

(assuming stellar mass is well-known, as it will be since to measure radial velocity we need exceptionally high S/N spectra of the star)

Observable is a measure of $m_p \sin(i)$

-> given v_{obs} , obtain a lower limit to the planetary mass

In absence of other constraints on the inclination, radial velocity searches provide lower limits on planetary masses

Magnitude of radial velocity:

Sun due to Jupiter: 12.5 m/s

Sun due to Earth: 0.1 m/s

i.e. *extremely small* - 10 m/s is Olympic 100m running pace

Spectrograph with a resolving power of 10^5 will have a pixel scale of the order of $10^{-5} c \sim \text{few km/s}$

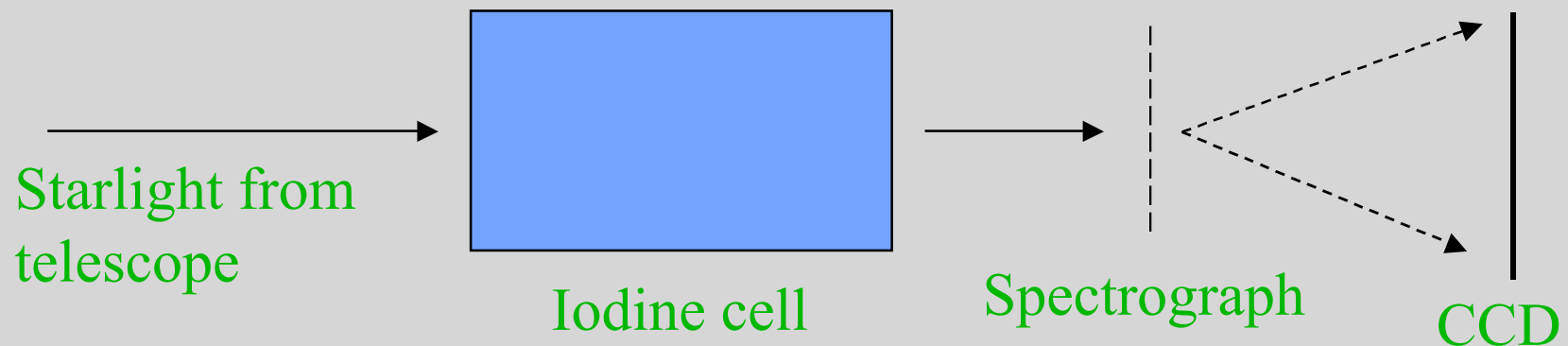
Specialized techniques that can measure radial velocity shifts of $\sim 10^{-3}$ of a pixel stably over many years are required

High sensitivity to small radial velocity shifts:

- Achieved by comparing high $S/N = 200 - 500$ spectra with template stellar spectra
- Large number of lines in spectrum allows shifts of much less than one pixel to be determined

Absolute wavelength calibration and stability over long timescales:

- Achieved by passing stellar light through a cell containing iodine, imprinting large number of additional lines of known wavelength into the spectrum
- Calibration suffers identical instrumental distortions as the data



Error sources

(1) Theoretical: photon noise limit

- flux in a pixel that receives N photons uncertain by $\sim N^{1/2}$
- implies absolute limit to measurement of radial velocity
- depends upon spectral type - more lines improve signal
- around 1 m/s for a G-type main sequence star with spectrum recorded at $S/N=200$
- practically, $S/N=200$ can be achieved for $V=8$ stars on a 3m class telescope in survey mode

(2) Practical:

- stellar activity - young or otherwise active stars are not stable at the m/s level and cannot be monitored with this technique
- remaining systematic errors in the observations

Currently, best observations typically achieve:

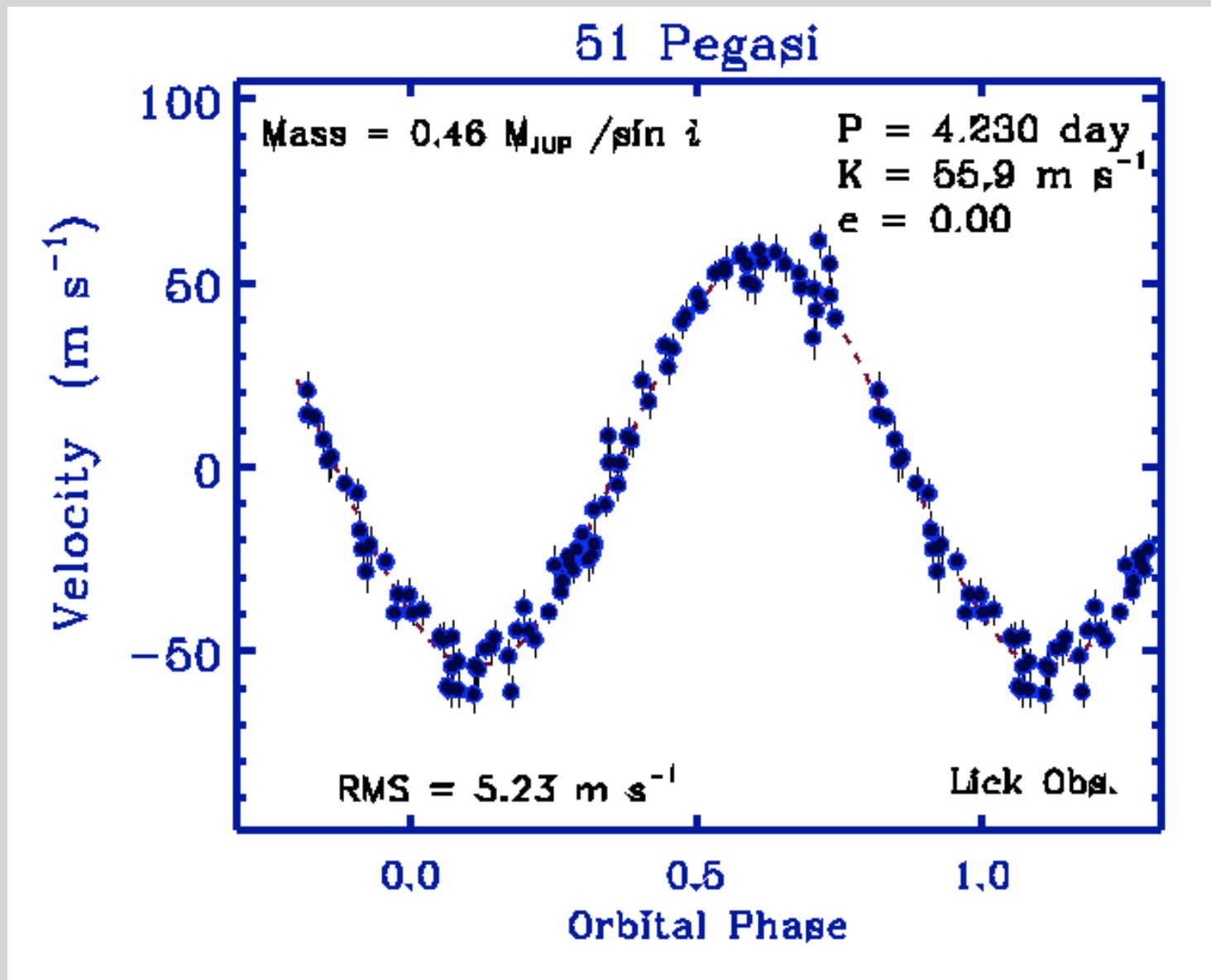
$$\sigma \approx 3 \text{ m/s}$$

...in a single measurement. However, the new high resolution echelle spectrograph HARPS (High Accuracy Radial velocity Planet Searcher) at the ESO La Silla 3.6m can achieve $\approx 1 \text{ m/s}$

47 Ursae Majoris c, inducing a radial velocity amplitude of 11.1 m/s, has one of the smallest amplitude wobbles so far attributed to a planet – the second planet to be found in this system!

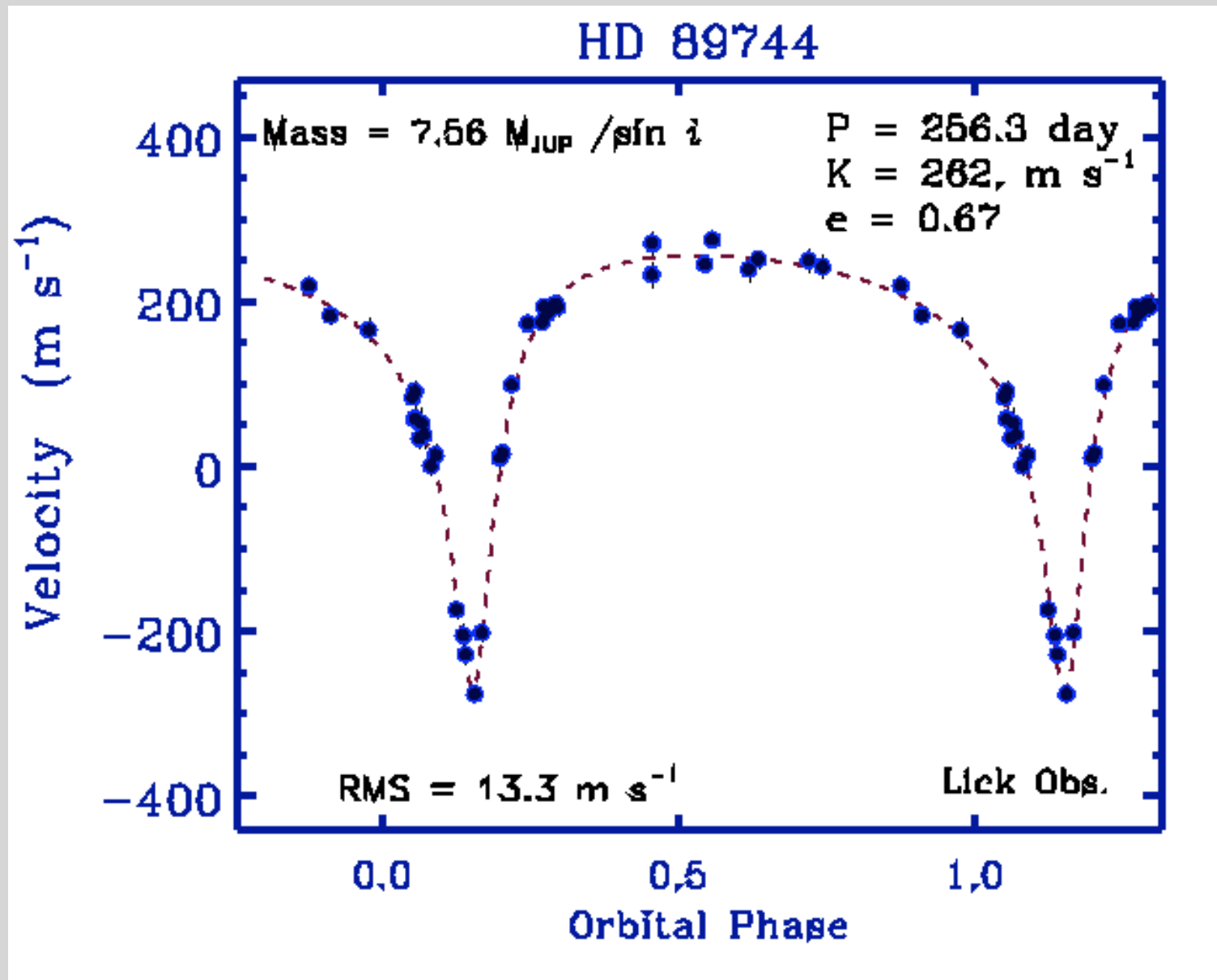
Radial velocity monitoring detects massive planets, especially those at small a , but is not sensitive enough to detect Earth-like planets at $\sim 1 \text{ AU}$.

Examples of radial velocity data

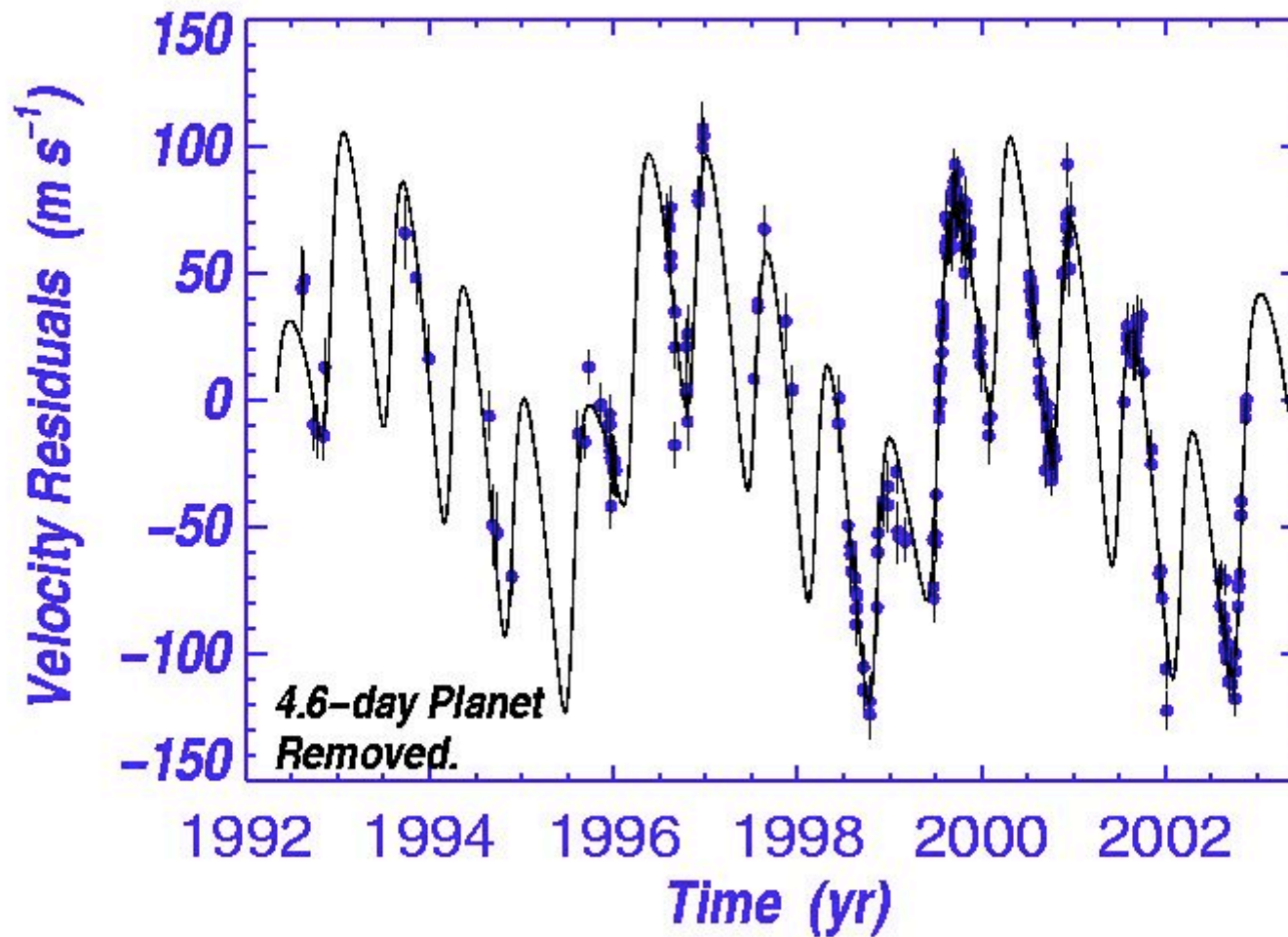


51 Peg, the first known exoplanet with a 4 day, circular orbit

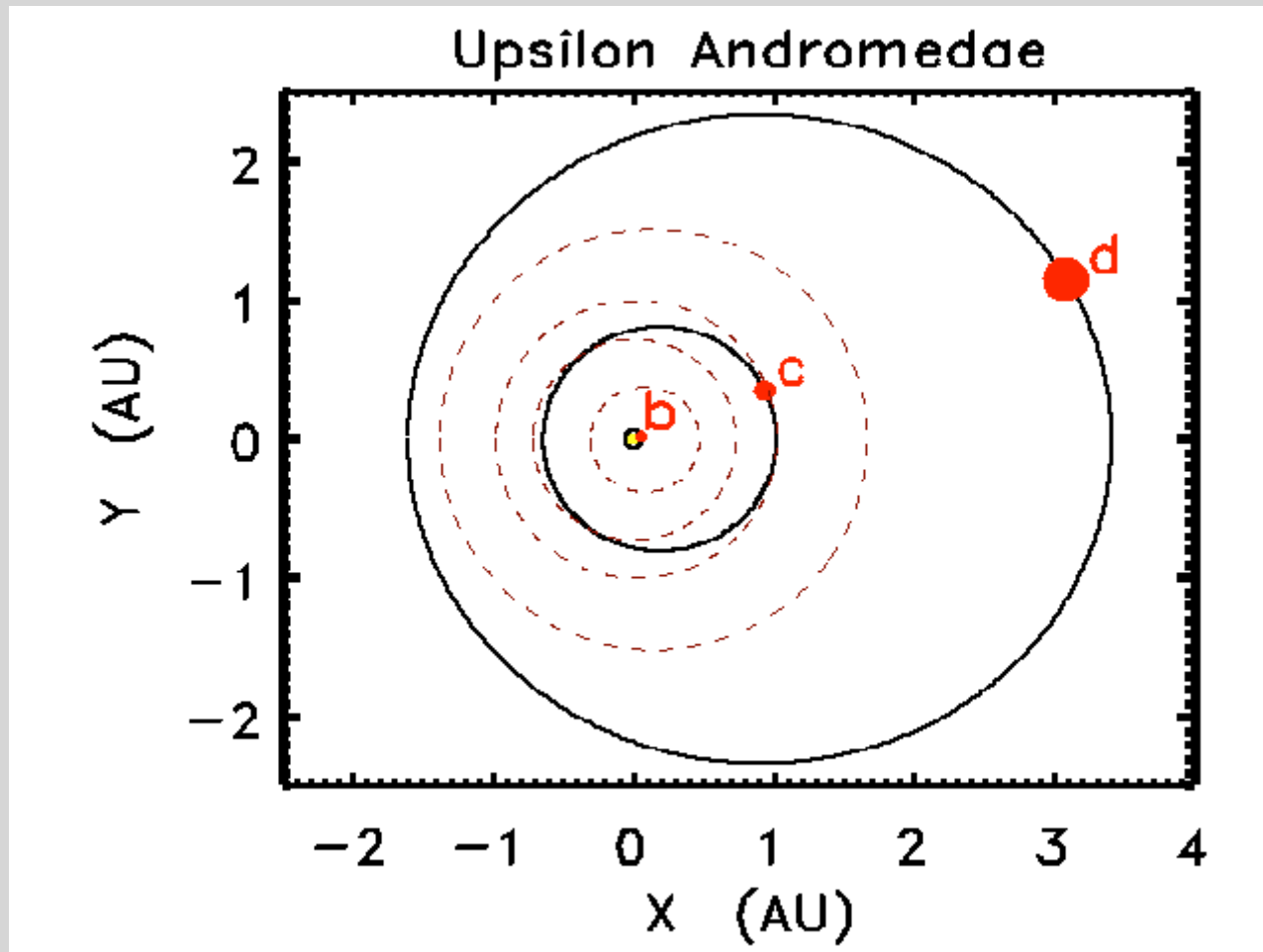
Example of a planet with an eccentric orbit: $e=0.67$



A Triple-Planet System Orbiting Upsilon Andromedae



A Triple-Planet System Orbiting Upsilon Andromedae



Summary: observables

- (1) Planet mass, up to an uncertainty from the normally unknown inclination of the orbit. Measure $m_p \sin(i)$
- (2) Orbital period \rightarrow radius of the orbit given the stellar mass
- (3) Eccentricity of the orbit

Summary: selection function

Need to observe full orbit of the planet: zero sensitivity to planets with $P > P_{\text{survey}}$

For $P < P_{\text{survey}}$, minimum mass planet detectable is one that produces a radial velocity signature of a few times the sensitivity of the experiment (this is a practical detection threshold)

$$m_p \sin(i) \propto a^{1/2}$$

Which planets are detectable?

